Trigonometric functions Cheat Sheet

Reciprocal trigonometric functions

Previously, you have met three trigonometric functions; *sinx*, *cosx* and *tanx*. This chapter introduces three more trigonometric functions, known as the reciprocal trigonometric

functions: • $secx = \frac{1}{cosx}$ (undefined for values of x for which cosx = 0)

> • $cosecx = \frac{1}{sinx}$ (undefined for values of x for which sinx = 0) • $cotx = \frac{1}{tanx}$ (undefined for values of x for which tanx = 0)

Since division by zero is undefined, we have that these functions are undefined when the denominators are equal to zero.

Note that $cotx = \frac{1}{tanx} = \frac{cosx}{sinx}$, simply by replacing tanx with $\frac{sinx}{cosx}$. This will sometimes be a more useful form to use.

Careful: It is not true that: $secx = (cosx)^{-1}$, $cosecx = (sinx)^{-1}$, $cotx = (tanx)^{-1}$ The negative power has a different meaning when used with trigonometric functions.

Graphing the reciprocal functions

You need to be able to sketch the reciprocal trigonometric functions as well as any transformations, using radians and degrees. Below are the graphs of the reciprocal functions





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We have two equations to solve. Using CAST or $x = 20.9^\circ$, 69.1°, 201°, 249° to 3 s.f.

a graphical method, our solutions are:

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using $sin^2x + cos^2x = 1$

A function only has an inverse if it is one-to-one. The trigonometric functions aren't one-to-one by definition, but if we restrict the domains, we can turn them into one-to-one functions. This allows us to define the inverse functions, which we can sketch by reflecting the *sinx*, *cosx* and *tanx* graphs in the line y = x.



Remember that since these functions are inverses, we have that arcsinx(sinx) = sin(arcsinx) = x. Of course, this works

Just like with the reciprocal functions, you may be asked to sketch a transformation of any of the inverse functions, or even



