

Solve the following equations, in the intervals given.

a $\sin 2\theta = \sin \theta, 0 \leq \theta \leq 2\pi$

b $\cos 2\theta = 1 - \cos \theta, -180^\circ < \theta \leq 180^\circ$

c $3\cos 2\theta = 2\cos^2 \theta, 0 \leq \theta < 360^\circ$

d $\sin 4\theta = \cos 2\theta, 0 \leq \theta \leq \pi$

e $3\cos \theta - \sin \frac{\theta}{2} - 1 = 0, 0 \leq \theta < 720^\circ$

f $\cos^2 \theta - \sin 2\theta = \sin^2 \theta, 0 \leq \theta \leq \pi$

g $2\sin \theta = \sec \theta, 0 \leq \theta \leq 2\pi$

h $2\sin 2\theta = 3\tan \theta, 0 \leq \theta < 360^\circ$

i $2\tan \theta = \sqrt{3}(1 - \tan \theta)(1 + \tan \theta), 0 \leq \theta \leq 2\pi$

j $\sin^2 \theta = 2\sin 2\theta, -180^\circ < \theta < 180^\circ$

k $4\tan \theta = \tan 2\theta, 0 \leq \theta \leq 360^\circ$

a $0, \frac{\pi}{3}, \pi, \frac{5\pi}{3}, 2\pi$

b $\pm 38.7^\circ$

c $30^\circ, 150^\circ, 210^\circ, 330^\circ$

d $\frac{\pi}{12}, \frac{\pi}{4}, \frac{5\pi}{12}, \frac{3\pi}{4}$

e $60^\circ, 300^\circ, 443.6^\circ, 636.4^\circ$

f $\frac{\pi}{8}, \frac{5\pi}{8}$

g $\frac{\pi}{4}, \frac{5\pi}{4}$

h $0^\circ, 30^\circ, 150^\circ, 180^\circ, 210^\circ, 330^\circ$

i $\frac{\pi}{6}, \frac{2\pi}{3}, \frac{7\pi}{6}, \frac{5\pi}{3}$

j $-104.0^\circ, 0^\circ, 76.0^\circ$

k $0^\circ, 35.3^\circ, 144.7^\circ, 180^\circ, 215.3^\circ, 324.7^\circ, 360^\circ$
51.3°