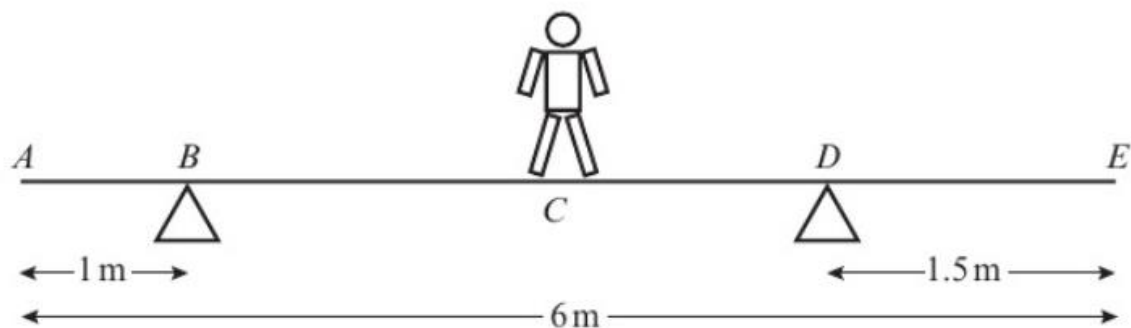




### Mixed exercise 4

- E 1** A plank  $AE$ , of length 6 m and weight 100 N, rests in a horizontal position on supports at  $B$  and  $D$ , where  $AB = 1$  m and  $DE = 1.5$  m. A child of weight 145 N stands at  $C$ , the midpoint of  $AE$ , as shown in the diagram. The child is modelled as a particle and the plank as a uniform rod. The child and the plank are in equilibrium. Calculate:

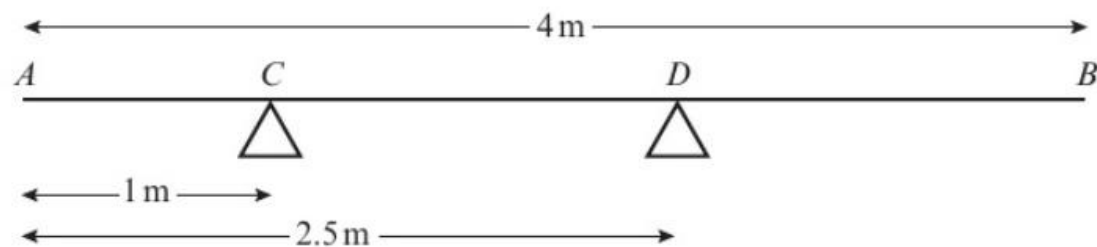


- a** the magnitude of the force exerted by the support on the plank at  $B$  **(3 marks)**
- b** the magnitude of the force exerted by the support on the plank at  $D$ . **(2 marks)**

The child now stands at a different point  $F$  on the plank. The plank is in equilibrium and on the point of tilting about  $D$ .

- c** Calculate the distance  $DF$ . **(4 marks)**

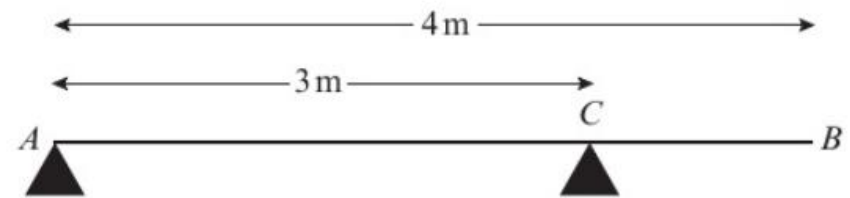
- E/P** 2 A uniform rod  $AB$  has length 4 m and weight 150 N. The rod rests in equilibrium in a horizontal position, smoothly supported at points  $C$  and  $D$ , where  $AC = 1$  m and



$AD = 2.5$  m as shown in the diagram. A particle of weight  $WN$  is attached to the rod at a point  $E$  where  $AE = x$  metres. The rod remains in equilibrium and the magnitude of the reaction at  $C$  is now equal to the magnitude of the reaction at  $D$ .

- a Show that  $W = \frac{150}{7 - 4x}$  **(6 marks)**
- b Hence deduce the range of possible values of  $x$ . **(3 marks)**

- E** 3 A uniform plank  $AB$  has mass  $40\text{ kg}$  and length  $4\text{ m}$ . It is supported in a horizontal position by two smooth pivots. One pivot is at the end  $A$  and the other is at the point  $C$  where  $AC = 3\text{ m}$ , as shown in the diagram.

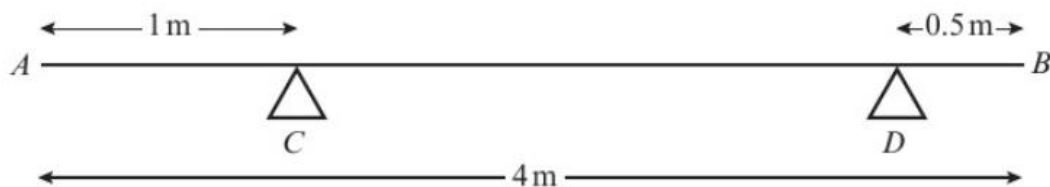


A man of mass  $80\text{ kg}$  stands on the plank which remains in equilibrium. The magnitude of the reaction at  $A$  is twice the magnitude of the reaction at  $C$ . The magnitude of the reaction at  $C$  is  $R\text{ N}$ . The plank is modelled as a rod and the man is modelled as a particle.

- a** Find the value of  $R$ . **(2 marks)**
- b** Find the distance of the man from  $A$ . **(3 marks)**
- c** State how you have used the modelling assumption that:
- i** the plank is uniform
  - ii** the plank is a rod
  - iii** the man is a particle. **(3 marks)**

**E/P**

**4** A non-uniform rod  $AB$  has length 4 m and weight 150 N. The rod rests horizontally in equilibrium on two smooth supports  $C$  and  $D$ , where



$AC = 1$  m and  $DB = 0.5$  m, as shown in the diagram. The centre of mass of  $AB$  is  $x$  metres from  $A$ . A particle of weight  $W$  N is placed on the rod at  $A$ . The rod remains in equilibrium and the magnitude of the reaction of  $C$  on the rod is 100 N.

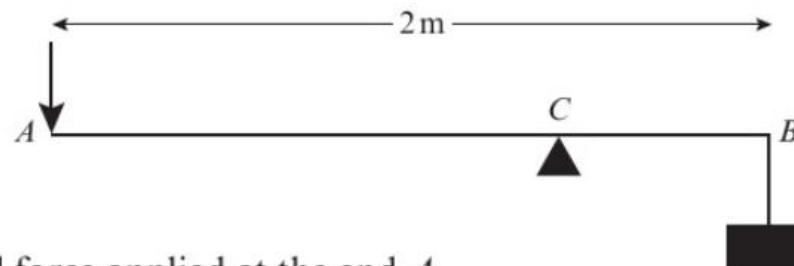
**a** Show that  $550 + 7W = 300x$ . **(4 marks)**

The particle is now removed from  $A$  and placed on the rod at  $B$ . The rod remains in equilibrium and the reaction of  $C$  on the rod now has magnitude 52 N.

**b** Obtain another equation connecting  $W$  and  $x$ . **(4 marks)**

**c** Calculate the value of  $x$  and the value of  $W$ . **(3 marks)**

- E** 5 A lever consists of a uniform steel rod  $AB$ , of weight  $100\text{ N}$  and length  $2\text{ m}$ , which rests on a small smooth pivot at a point  $C$ . A load of weight  $1700\text{ N}$  is suspended from the end  $B$  of the rod by a rope. The lever is held in equilibrium in a horizontal position by a vertical force applied at the end  $A$ , as shown in the diagram. The rope is modelled as a light string.



- a** Given that  $BC = 0.25\text{ m}$  find the magnitude of the force applied at  $A$ . **(4 marks)**
- The position of the pivot is changed so that the rod remains in equilibrium when the force at  $A$  has magnitude  $150\text{ N}$ .
- b** Find, to the nearest centimetre, the new distance of the pivot from  $B$ . **(4 marks)**

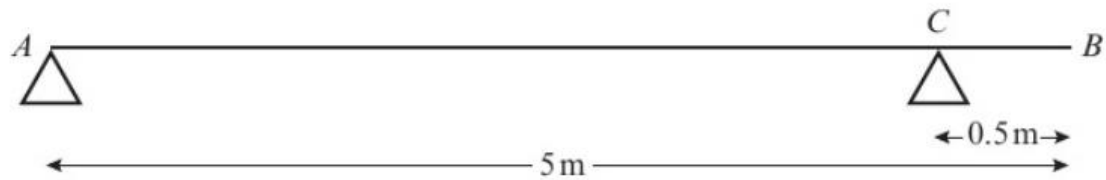
- E** 6 A plank  $AB$  has length  $4\text{ m}$ . It lies on a horizontal platform, with the end  $A$  lying on the platform and the end  $B$  projecting over the edge, as shown in the diagram. The edge of the platform is at the point  $C$ .



Jack and Jill are experimenting with the plank. Jack has mass  $48\text{ kg}$  and Jill has mass  $36\text{ kg}$ . They discover that if Jack stands at  $B$  and Jill stands at  $A$  and  $BC = 1.8\text{ m}$ , the plank is in equilibrium and on the point of tilting about  $C$ .

- a** By modelling the plank as a uniform rod, and Jack and Jill as particles, find the mass of the plank. **(4 marks)**
- They now alter the position of the plank in relation to the platform so that, when Jill stands at  $B$  and Jack stands at  $A$ , the plank is again in equilibrium and on the point of tilting about  $C$ .
- b** Find the distance  $BC$  in this position. **(4 marks)**

- E** 7 A plank of wood  $AB$  has mass  $12\text{ kg}$  and length  $5\text{ m}$ . It rests in a horizontal position on two smooth



supports. One support is at the end  $A$ . The other is at the point  $C$ ,  $0.5\text{ m}$  from  $B$ , as shown in the diagram. A girl of mass  $30\text{ kg}$  stands at  $B$  with the plank in equilibrium.

- a** By modelling the plank as a uniform rod and the girl as a particle, find the reaction on the plank at  $A$ . **(4 marks)**

The girl gets off the plank. A boulder of mass  $m\text{ kg}$  is placed on the plank at  $A$  and a man of mass  $93\text{ kg}$  stands on the plank at  $B$ . The plank remains in equilibrium and is on the point of tilting about  $C$ .

- b** By modelling the plank again as a uniform rod, and the man and the boulder as particles, find the value of  $m$ . **(5 marks)**

- E/P** 8 A plank  $AB$  has mass  $50\text{ kg}$  and length  $4\text{ m}$ . A load of mass  $25\text{ kg}$  is attached to the plank at  $B$ . The loaded plank is held in equilibrium, with  $AB$  horizontal, by two vertical ropes attached at  $A$  and  $C$ , as shown in the diagram. The plank is modelled as a uniform rod and the load as a particle. Given that the tension in the rope at  $C$  is four times the tension in the rope at  $A$ , calculate the distance  $CB$ . **(7 marks)**

