Wednesday afternoon quiz

(i) Given $x = \tan^2 4y$, $0 < y < \frac{\pi}{8}$, find $\frac{dy}{dx}$ as a function of x.

Write your answer in the form $\frac{1}{A(x^p + x^q)}$, where A, p and q are constants to be found.

(5)

(ii) The volume V of a cube is increasing at a constant rate of 2 cm 3 s $^{-1}$. Find the rate at which the length of the edge of the cube is increasing when the volume of the cube is 64 cm 3 .

(5)

Name The School



1 2 3



4 5

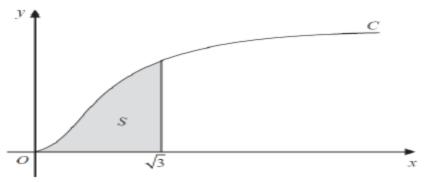


Figure 4

Figure 4 shows a sketch of part of the curve C with equation

$$y = \frac{x^2 \ln x}{3} - 2x + 4$$
, $x > 0$

The finite region S, shown shaded in Figure 4, is bounded by the curve C, the x-axis and the lines with equations x = 1 and x = 3.

(a) Complete the table below with the value of y corresponding to x = 2. Give your answer to 4 decimal places.

x	1	1.5	2	2.5	3
y	2	1.3041		0.9089	1.2958

(1)

(b) Use the trapezium rule, with all the values of y in the completed table, to obtain an estimate for the area of S, giving your answer to 3 decimal places.

(3)

(c) Use calculus to find the exact area of S.

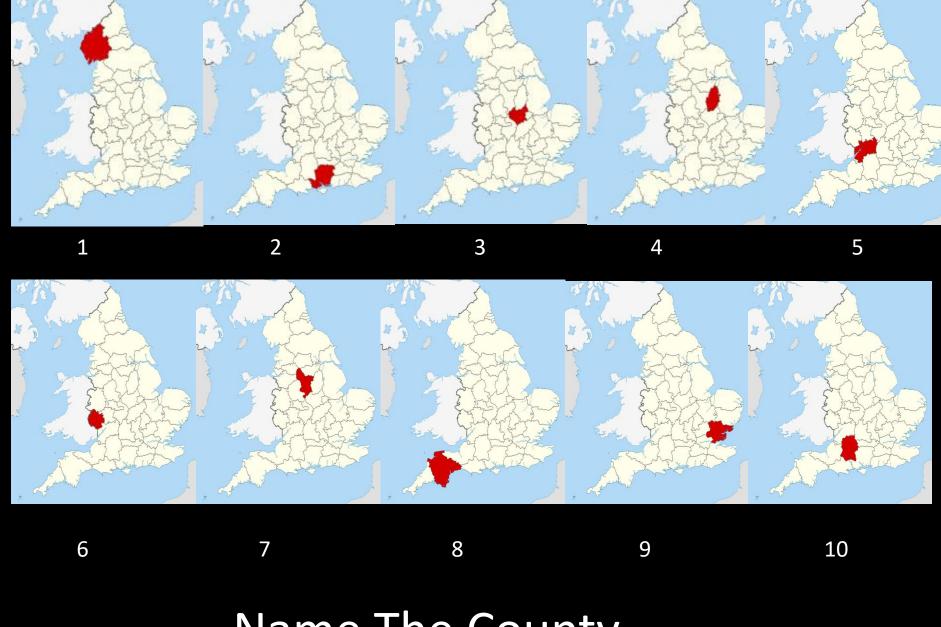
Give your answer in the form $\frac{a}{b} + \ln c$, where a, b and c are integers.

(6)

(2)

(1)

- (d) Hence calculate the percentage error in using your answer to part (b) to estimate the area of S. Give your answer to one decimal place.
- (e) Explain how the trapezium rule could be used to obtain a more accurate estimate for the area of S.



Name The County

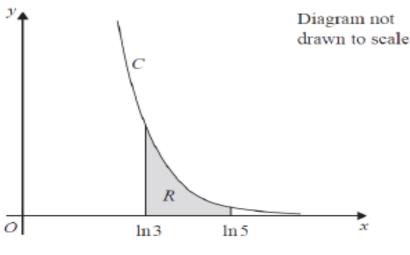


Figure 2

The curve C has parametric equations

$$x = \ln(t+2), \quad y = \frac{4}{t^2} \quad t > 0$$

The finite region R, shown shaded in Figure 2, is bounded by the curve C, the x-axis and the lines with equations $x = \ln 3$ and $x = \ln 5$.

(a) Show that the area of R is given by the integral

The integral State p
$$\int_{1}^{3} \frac{dt}{t^{2}(t+1)} dt$$
and q
(3)

(b) Hence find an exact value for the area of R.

Write your answer in the form $(a + \ln b)$, where a and b are rational numbers.

(7)

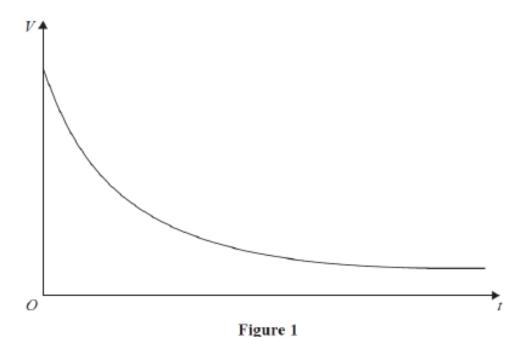
(c) Find a cartesian equation of the curve C in the form y = f(x).

(2)

Solve these equations

For every equation, solve for $0 \le x \le 360^{\circ}$

- 1) $\sin x + \cos x = 0$
- 2) $\cot x = 0$
- 3) $\sin x = 0.5$
- 4) $\sec x = 0$
- 5) $3 \sin x + 4 \cos x = 6$



The value of Lin's car is modelled by the formula

$$V = 18\,000e^{-0.2t} + 4000e^{-0.1t} + 1000, \quad t \ge 0$$

where the value of the car is V pounds when the age of the car is t years.

A sketch of t against V is shown in Figure 1.

(a) State the range of V.

(2)

According to this model,

(b) find the rate at which the value of the car is decreasing when t = 10. Give your answer in pounds per year.

(3)

(c) Calculate the exact value of t when V = 15 000.

(4)

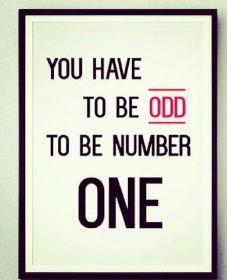
An opinion without

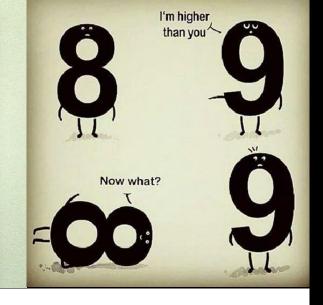
3.14159

is just an onion.









Teacher asks student: What is the half of 8?

Student: Miss horizontally or vertically?

Teacher: What do mean?

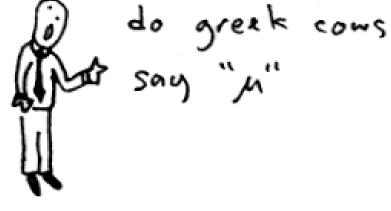
Student: Horizontally it is o and vertically it



is 3.

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How many of these jokes are funny?