

$$f(x) = |3x + 2|, \quad x \in \mathbb{R}.$$

- a) Sketch the graph of $f(x)$, clearly indicating the coordinates of any points where the graph of $f(x)$ meets the coordinate axes.
- b) Solve the equation

$$f(x) = 1.$$

$$\boxed{}, \quad \boxed{(0, 2), \left(-\frac{2}{3}, 0\right)}, \quad \boxed{x = -\frac{1}{3}, -1}$$

The functions f and g are defined as

$$f(x) = |2x - 4|, \quad x \in \mathbb{R}$$

$$g(x) = |x|, \quad x \in \mathbb{R}.$$

- a) Sketch in the same diagram the graph of f and the graph of g .
Mark clearly in the sketch the coordinates of any x or y intercepts.
- b) Solve the equation

$$f(x) = g(x).$$

- c) Hence, or otherwise, solve the inequality

$$f(x) < g(x).$$

$$\boxed{(0, 0), (2, 0), (0, 4)}, \quad \boxed{x = \frac{4}{3}, 4}, \quad \boxed{\frac{4}{3} < x < 4}$$

Question 11 (*)**

Solve the modulus inequality

$$12 - 2|2x - 3| \geq 7.$$

$$\boxed{\frac{1}{4} \leq x \leq \frac{11}{4}}$$

Question 12 (*)**

Solve the modulus equation

$$4x + |3x + 2| = 1.$$

$$\boxed{}, \quad \boxed{x = -\frac{1}{7}}$$

Question 13 (*)**

Find the solutions of the equation

$$|2x^2 - 5| = 13.$$

$$\boxed{x = \pm 3}$$

The curve C_1 and the curve C_2 have respective equations

$$y = |x| \quad \text{and} \quad y = |x - 2| + 1.$$

- Sketch the graph of C_2 , indicating the coordinates of any intercepts with the coordinate axes.
- Determine the coordinates of the point of intersection between the graph of C_1 and the graph of C_2 .

$$\boxed{\left(\frac{3}{2}, \frac{3}{2}\right)}$$

Question 53 (****)

The straight line L with equation

$$y = x + 3, \quad x \in \mathbb{R},$$

intersects the curve C with equation

$$y = |x^2 - 9|, \quad x \in \mathbb{R},$$

at three distinct points.

- a) Sketch on the same set of axes the graph of L and the graph of C .
The sketch must include the coordinates of any x or y intercepts.
- b) Find the coordinates of the points of intersections between L and C .

$$\boxed{(-3,0), (3,0), (0,3), (0,9)}, \quad \boxed{(-3,0), (2,5), (4,7)}$$

